

Effects of Non-linearity in Storage-discharge Relationship on Design Flood Estimates

A Rahman and A Goonetilleke

*Physical Infrastructure Centre, School of Civil Engineering, Queensland University of Technology
(a.rahman@qut.edu.au)*

Abstract: Rainfall-based flood estimation techniques are commonly adopted in hydrological design. Runoff routing models are widely used in Australia, which use either a linear or nonlinear storage-discharge relationship. Australian Rainfall and Runoff recommends the use of a nonlinear storage-discharge relationship; though, many have proposed other types of storage-discharge relationships. This paper adopts a Monte Carlo simulation technique to examine the effects of nonlinearity in storage-discharge relationship on design flood estimates. This simulates thousands of rainfall events, which are then routed through a runoff routing model to generate streamflow hydrographs. The nonlinearity parameter in the storage discharge relationship is varied to quantify its effects on design flood estimates. It is found that nonlinearity parameter has significant effect on design floods, particularly for larger floods. Results from three study catchments indicate that a nonlinear storage-discharge relationship is preferable to linear relationship.

Keywords: Runoff routing; Storage-discharge relationship; Flood estimation; Design floods.

1. INTRODUCTION

In rainfall-based flood estimation techniques, runoff routing models are commonly adopted e.g. RORB [Laurenson and Mein, 1997], WBNM [Boyd et al., 1987 and Rigby et al., 1999], RAFTS [Willing and Partners, 1988], URBS [Carroll, 1994]. A central component of these models is a conceptual storage and storage routing procedure. Australian Rainfall and Runoff [I. E. Aust., 2001] recommends to use a nonlinear storage-discharge relationship for estimation of large floods. Some investigators have proposed other forms of storage-discharge relationships. For example, Bates and Pilgrim [1983] proposed an asymptotically linear relationship. Sriwongsitanon et al. [1998] proposed a nonlinear relationship with an intercept and Zhang and Cordery [1999] proposed a linear relationship. Wong [1989] and Bates et al. [1993] had limited success in establishing variation patterns between optimal parameter values of k_c and m of RORM model. Bates and Pilgrim [1986] describe a nonlinear runoff routing model with a storage-discharge relation different from the power law function, which approximates linear behaviour at high flows. RORB model has also provisions to adopt

storage-discharge relationships different from the power function. However, little use has yet been made of these alternative forms of storage-discharge relations (I. E. Aust., 2001). The question as to whether the nonlinear storage-discharge relationship is appropriate for estimation of large floods has never been answered [Zhang, 2000].

This paper presents an empirical study to assess the effects of nonlinearity in storage-discharge relationship on design flood estimates. This uses a large number of simulated rainfall events with a simple conceptual storage model to examine the effects of nonlinearity on design floods covering a large range of frequency.

2. APPROACH

A simple storage-discharge relationship is adopted in this study, expressed by:

$$S = kQ^m \quad (1)$$

where S is catchment storage in m^3 , k is storage delay parameter in hour, Q is the rate of outflow in

m^3/s and m is a nonlinearity parameter. This model becomes linear when $m = 1$. The value of m is generally taken as 0.80 for many applications. This study examines three values of m , which are 0.8, 0.9 and 1.0.

To examine the effects of assumed storage-discharge relationship on floods having a large range of frequency; rainfall events are simulated using a Monte Carlo Simulation technique. This generates 3 to 6 partial series rainfall events per year, which have the potential to produce significant surface runoff. From the observed pluviograph data, independent rainfall events are identified as a period of rainfall preceded and followed by at least 6 consecutive hours of no rainfall, following the approach of Hoang et al. [1999]. For each complete storm, a rainfall burst (called storm-core) is identified, which has the highest rainfall intensity ratio compared to the 2-year average recurrence interval (ARI) design rainfall [Hoang et al., 1999; Rahman et al., 2001a,b].

The distribution of storm-core duration (D_c) is obtained from the historical pluviograph data recorded on the catchment, the distribution of rainfall intensity (I_c) is expressed in the form of intensity-frequency-duration (IFD) curves and observed temporal patterns (TP_c) of storm-core events are expressed in dimensionless form and stored in a data bank for random selection during event simulation.

An initial loss continuing loss model is used for runoff production. The values of initial losses are computed from historical concurrent pluviograph and streamflow data. A theoretical distribution is fitted to IL_c data. Continuing loss (CL_c) is assumed to be constant from rainfall event to event for a catchment.

In the simulation of a rainfall event, a value of D_c is generated, followed by generation of I_c and random selection of TP_c depending on generated D_c value. These form a gross rainfall hyetograph, as shown in Figure 1. A value of IL_c is then generated, which together with fixed CL_c , form net rainfall hyetograph. A large number of rainfall hyetographs (in the order of thousands) are simulated. The adopted Monte Carlo Simulation technique is described in more detail in Rahman et al. [2001a,b]. These simulated rainfall hyetographs are then routed through the runoff routing model with different sets of (m, k) values to obtain streamflow hydrographs. The peaks of these hydrographs are noted and subjected to a non-parametric frequency analysis to construct a derived flood frequency curve. The derived flood

frequency curves for different sets of (m, k) values are plotted to examine the effects of nonlinearity (m) on design floods.

3. STUDY CATCHMENTS

Three catchments from Victoria are selected: Avoca River at Amphitheatre (catchment area, $A = 78 \text{ km}^2$), Boggy Creek at Angleside ($A = 108 \text{ km}^2$) and Tarwin River East Branch at Dumbalk ($A = 127 \text{ km}^2$). These are unregulated and rural catchments.

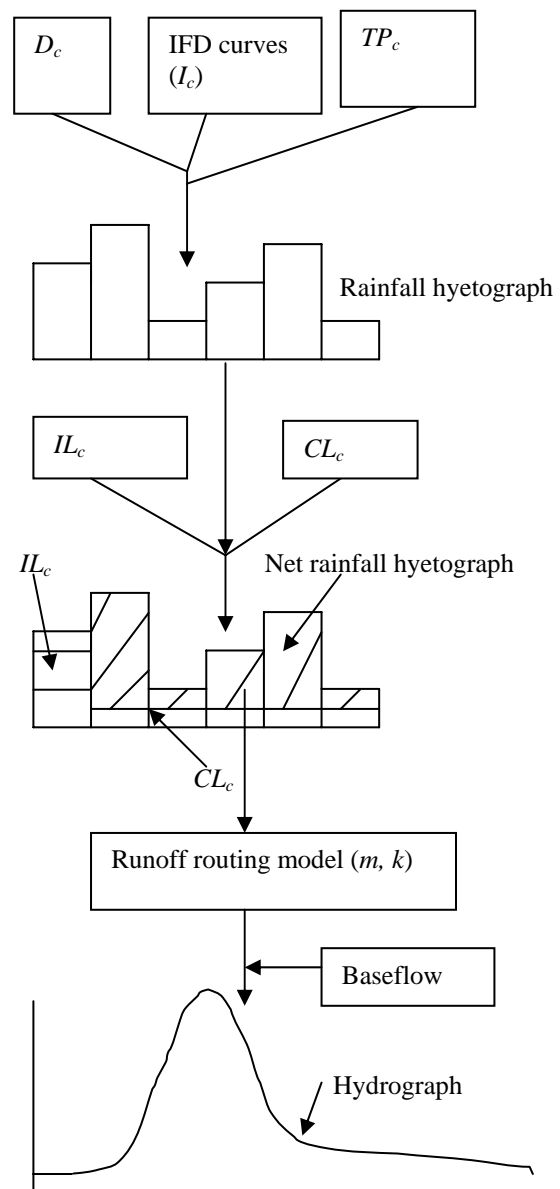


Figure 1. Rainfall and streamflow events simulation.

4. RESULTS

Three values of m are considered, $m = 1.0$ (linear storage-discharge relationship), $m = 0.8$ (nonlinear storage-discharge relation, frequently adopted in RORB model) and an intermediate value, $m = 0.9$. Since, k value changes with m , a different k was obtained for each m value from calibration of the runoff routing model. For each catchment, a number of observed pluviograph and streamflow events were selected for calibration. Three sets of (m, k) values were obtained for each of the three catchments, as shown in Table 1. The k values were found to be consistent with the recommended adjusting factor, $(Q_p/2)^{m-m1}$, where Q_p is the peak discharge and m the old and $m1$ the new value of m [Laurenson and Mein, 1997].

Table 1. Values of (m, k) from calibration.

Catchment	Set 1	Set 2	Set 3
Avoca River	(1.0, 7)	(0.9, 9)	(0.8, 13)
Boggy Creek	(1.0, 17)	(0.9, 24)	(0.8, 34)
Tarwin River	(1.0, 14)	(0.9, 20)	(0.8, 27)

A derived flood frequency curve was constructed for a catchment from 10,000 simulated rainfall and streamflow events for each set of (m, k) values. An input rainfall hyetograph and other variables/parameters (e.g. CL , baseflow) remain same for a catchment in three runs with three sets of (m, k) values, which allows examining the effects of changing m value on design floods.

The derived flood frequency curves for Avoca River, Boggy Creek and Tarwin River catchments are shown in Figures 2, 3 and 4, respectively. These show that flood peaks with different m values do not vary noticeably at smaller ARIs (up to about 10 year), but there are remarkable differences for greater ARIs. The percentage differences in flood magnitudes from linear storage-discharge relationship ($m = 1$) and two other degrees of nonlinearities ($m = 0.9$ and $m = 0.8$) were found to be remarkably high, particularly at higher ARIs, as shown in Figure 5. The above results indicate that flood frequency curves are remarkably sensitive to the adopted m value, particularly at higher ARIs.

The observed partial series flood data at the selected catchments are superimposed on Figures 2-4. For Avoca River catchment (Figure 2), it appears that for up to 10 year ARI floods, $m = 0.8$ better approximates the observed flood series. For ARIs greater than 10 years, a greater m value tends

to better approximate the observed flood series. It may be noted that the observed largest flood data for Avoca River catchment does not match well with the remaining historical flood data, and hence might have been subjected to data error. Ignoring this data point, $m = 0.9$ appears to best approximate the observed flood series.

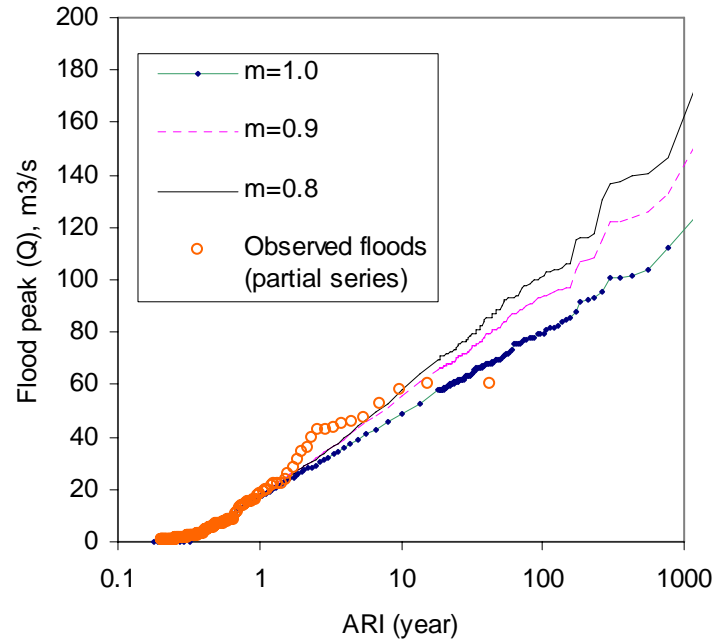


Figure 2. Effects of changing m on flood peaks for Avoca River catchment.

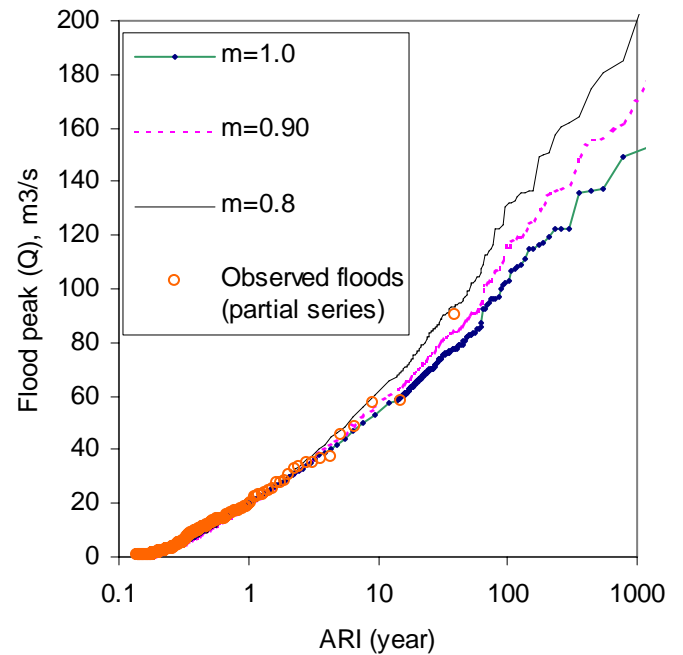


Figure 3. Effects of changing m on flood peaks for Boggy River catchment.

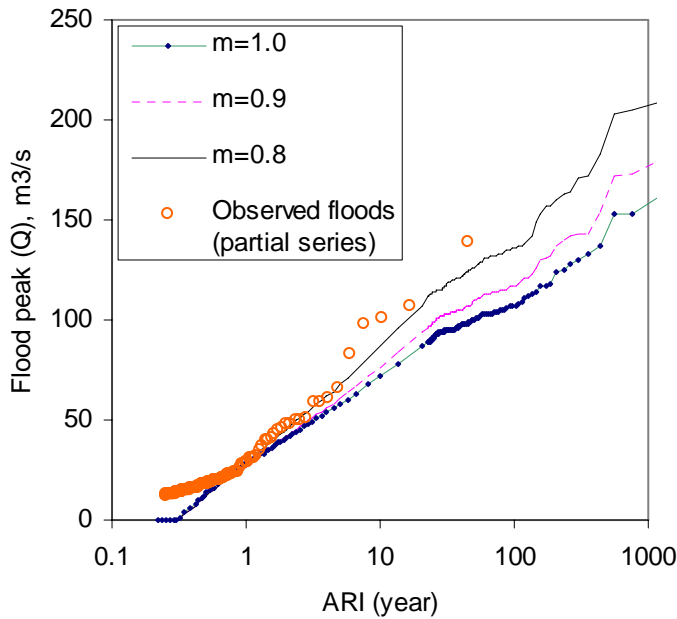


Figure 4. Effects of changing m on flood peaks for Tarwin River catchment.

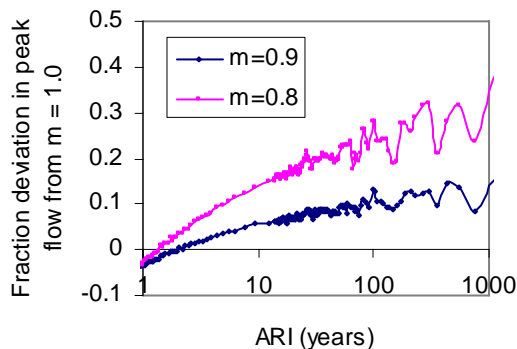


Figure 5. Fraction deviation in peak floods from linearity ($m = 1.0$) to nonlinearities, $m = 0.9$ and $m = 0.8$ (Boggy Creek catchment).

For Boggy Creek catchment (Figure 3), it is found that $m = 0.9$ best approximates the observed flood series. For Tarwin River catchment, it appears that $m = 0.8$ best approximates the observed flood series. It should be noted here that there are only few data points in the observed flood series beyond 20 years ARI, which makes it difficult to assess the suitability of an m value for larger floods.

5. CONCLUSION

The paper presents an empirical study to identify an appropriate value of the exponent m in the

storage-discharge relationship for the runoff routing models. Following conclusions may be drawn from the study:

- Flood peaks generated by the runoff routing models are quite sensitive to the m value, particularly for large floods.
- For the three study catchments, a nonlinear storage-discharge relationship appears to better approximate the observed flood series than the linear relationship.
- There is no unique m value that is equally valid for all the three study catchments. This indicates the importance of determining an appropriate m value for a particular catchment.
- Monte Carlo simulation technique offers a powerful means to determine an appropriate m value for a particular catchment covering a wide range of flood frequencies.

6. REFERENCES

- Bates, B.C., and D.H. Pilgrim, Investigation of storage-discharge relations for river reaches and runoff routing models. *Civil Eng. Trans.* IEAust, CE25(3): 153-161, 1983.
- Bates, B.C. and D.H. Pilgrim, Simple models for nonlinear runoff routing. *Civil Eng. Trans.*, IEAust, CE28:284-291, 1986.
- Bates, B.C., N.R. Sumner and M.J. Boyd., Non-linearity of flood runoff: what can be gleaned from calibrated runoff routing models? *Civil Eng. Trans.*, IEAust, CE35(2): 151-164, 1993.
- Boyd, M.J., B.C. Bates, D.H. Pilgrim and I. Cordery, WBNM a general runoff routing model computer programs and user guide. Water Research Lab. Report No. 170. The University of New South Wales, 1987.
- Carroll, D.G., The BCC Catchment Management Runoff Routing Model Manual, Version 3.3, Brisbane City Council, Brisbane, Australia, 1994.
- Hoang, T.M.T., A. Rahman, P.E. Weinmann, E.M. Laurenson and R.J. Nathan, Joint probability description of design rainfalls. In *Proc. Hydro. and Water Resour. Symp.*, I.E. Aust., Brisbane, Vol. 1, pp 379-384, 1999.
- Institution of Engineers Australia, Australian Rainfall and Runoff - a guide to flood estimation., 2001.
- Laurenson, E.M. and R.G. Mein, RORB Version 4 Runoff Routing Program Use Manual, Dept. of Civil Eng., Monash University, 1997.
- Rahman, A., P.E. Weinmann, T.M.T. Hoang, E.M. Laurenson and R.J. Nathan, Monte Carlo Simulation of Flood Frequency Curves from Rainfall. Report 01/4. CRC for Catchment Hydrology, Monash University, 2001a.

- Rahman, A., P.E. Weinmann, T.M.T. Hoang, E.M. Laurenson, Monte Carlo Simulation of Flood Frequency Curves from Rainfall. *Journal of Hydrology*. (In press), 2001b.
- Rigby, E.H., M.J. Boyd and R. VanDire, Experiences in developing the hydrology model: WBNM2000, Proc. 8th Intl. conf. on urban storm drainage, 1374-1381, ed by I. B. Joliffe and J. E. Ball, Sydney, 1999.
- Sriwongsitanon, N., J.E. Ball and I. Cordery, An investigation of the relationship between the flood wave speed and parameters in runoff routing models. *Hydrological Sciences J*, 43(2): 197-213, 1998.
- Willing and partners Pty Ltd, RAFTS-runoff analysis and flow training system, detailed documentation and user manual, version 2.5, 1988.
- Wong, T.H.F., Non-linearity in catchment flood response. *Civil Eng. Trans. IEAust. CE31(1)*: 30-37, 1989.
- Zhang, S.Y. and I. Cordery, The catchment storage-discharge relationship: nonlinear or linear? *Australian Journal of Water Resources*, 3(1): 155-165, 1999.
- Zhang, S.Y., I. Cordery and A. Sharma, A volume law for specification of linear channel storage for estimation of large floods, *Water Resour. Res*, 36(6): 1535-1543, 2000.